# Parallel Prefix Adder in QCA technology

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# Why quantum-dot automata

- Transistor physical limitation;
- High speed circuits;
- Natural pipelined;
- The information is propagated using the eletric field.

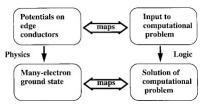


Figure: QCA Cell



# **Basics**

- Each cell has 4 dots and 2 eletrons;
- Based in three devices: Wire, Majority Gate and Inverter.

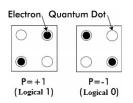
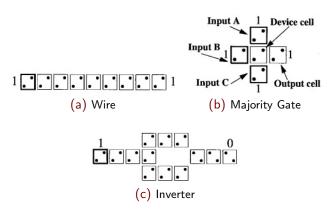


Figure: Technologic mapping



## **Devices**







#### Parallel Prefix Adder

### PPA Algorithm

- **1** Calculate  $P_i$  and  $G_i$ :  $P_i = a_i \oplus b_i$  and  $G_i = a_i \cdot b_i$
- **2** Calculate the group generation and the group propagation using the following expressions:  $G_{i+1,i} = G_{i+1} + P_{i+1} \cdot G_i$  and  $P_{i+1,i} = P_{i+1} \cdot P_i$
- **3** Calculate the Couts for each bit:  $Cout_{i-1} = G_{i,0} + P_{i,0} \cdot C_{in}$
- **4** Calculate the sum for each bit  $S_i = P_i \oplus Cout_{i-1}$



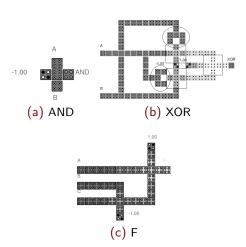
# Majority Equations

### Principal Translations

- $OR = a + b \Rightarrow M(a, b, 1)$
- $\bullet (G_1, P_{i+1,i}) AND = a \cdot b \Rightarrow M(a, b, 0);$
- $(P_i, S_i) \ XOR = a \oplus b = a \cdot (b) + (a) \cdot b \Rightarrow M(M(a, b, 0), M(a, b, 0), 1);$
- $(Cout_{i-1}, G_{i+1,i}) F = a + b \cdot c \Rightarrow M(A, M(B, C, 0), 1).$



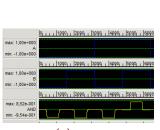
### Circuits

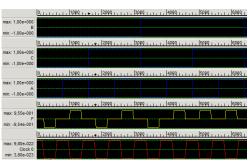






### Wave Form





(a) AND

(b) XOR

Figure: Wave Forms



#### Conclusions

- This paper presents ...
  - Majority Equations to each PPA cell;
  - Implementation of each PPA cell using QCA Technology.
- Future works ...
  - Full implementations of PPA with 4 bits;
  - Develop a strategy to assembly and route all cells of a more complex circuit;
  - Comparison with adders in literature.



# Acknowledgments

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