# Multiagent Systems and Agent-based Modeling and Simulation

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#### About me...

- PhD University of Karlsruhe, Germany
- doing Multiagent Systems (MAS): since 1993
- member of IFAAMAS board (2004–2008, 2014–current)
- chair AAMAS 2014 conf. in Paris
- plenary speaker AAMAS 2017
- assoc. editor JAAMAS (Kluver/Springer) from 2010 to 2017
- assoc. editor Adv. in Complex Systems from 2007 to 2017
- organization of several workshops and meetings around MAS, machine learning and complex systems



#### What my group does...

- Approaches
  - Multiagent reinforcement learning
  - Coordination in MAS
  - Game theoretic decision making
  - Self organization using swarm intelligence
  - Agent-based modeling and simulation (ABMS)
  - Complex systems; networks
- Applications
  - Traffic: control and routing
  - Task allocation in MAS
  - Smart cities
  - History and teledramaturgy



### What you can expect from this tutorial

- Traditional AI versus distributed AI
- Overview on multiagent AI: autonomous agents and multiagent systems
- Discussion about which problems arise when a system has more than one interacting agent
- Overview on agent-based modeling and simulation (ABMS)
- Cross-fertilization: evolutionary algorithms and multiagent systems
- Review on works in the frontier
- Open challenges



#### Recommended Reading

- Shoham and Leyton-Brown: Multiagent Systems
- M. Wooldridge: Multiagent Systems
- Nikos Vlassis: A Concise Introduction to Multiagent Systems and Distributed AI
- Stone, P. and Veloso, M.: Multiagent systems: a survey from a machine learning perspective. Autonomous Robots, 8(3), 2000
- Leyton-Brown and Shoham: Essentials of Game Theory
- Articles in conferences and workshops: AAMAS, IJCAI, AAAI, ICML, EcoMAS, ALA, OptMAS



#### **Outline**

- 1 Overview
- 2 Introduction to AA & MAS
  - The Basics of AA and MAS
    - Monoagent vs. Multiagent AI
    - Multiagent Systems
- 3 Agent-based Modeling and Simulation
- 4 Planning and MDP
  - Sequential Planning and Decision Making for One Agent: MDP
  - Sequential Decision Making in MASs: MMDP / SG
- Reinforcement Learning

  Basics
  - Single-agent RL
  - Multiagent RL
- 6 Distributed Constraint Optimization
  - CSP and COP
  - DisCSP and DCOP
- 7 Integration ML and MAS
  - Agent-Based ML
  - ML in MASs
- 8 Challenges
- 9 References



#### **Outline and Goals**

- Kernel: show differences between single and multi agent AI
- Also: agent-based modeling and simulation
- 3 main areas of Al are (re)visited here (those closer to PPSN's topics)
  - Planning and decision making (mostly Markov decision processes)
  - Learning (mostly reinforcement learning)
  - Problem solving via constraint satisfaction



LThe Basics of AA and MAS

### Why AA and MAS?

- Decentralization: "the" rule in Nature
  - no leader in flocks of birds
  - no leader in colonies of ants (queen just lay eggs!)
  - ...
  - why people always think that a pattern exists only if someone creates or orchestrates it ???



L The Basics of AA and MAS

## Mono vs. Multiagent

Example Figure Skating

one agent	multiagent			not as planned!
	T	No.	<b>M</b>	



The Basics of AA and MAS

#### **Lessons Learned**

- One agent is easy (well...)
- Two agents: coordination !!!
- But: not all situations can be predicted...
- Therefore adaptation is key



# What's an Agent?

- No standard, accepted definition
- Def. 1:

An autonomous agent is a system situated within and a part of an environment that senses that environment and acts on it, over time, in pursuit of its own agenda and so as to affect what it senses in the future. (Franklin and Graesser)



The Basics of AA and MAS

## What's an Agent?

Def. 2:

An agent is a computer system that is situated in some environment and that is capable of independent (autonomous) action in this environment on behalf of its user or owner (figuring out what needs to be done to satisfy design objectives, rather than constantly being told) (Wooldridge)



The Basics of AA and MAS

# What's an Agent?

- (other) important concepts:
  - Situated
  - On behalf of its owner
  - Rather than constantly being told
  - Should be able to:
    - Perceive the environment
    - 2 Decide which action to make (deliberation)
    - Act in the environment



L The Basics of AA and MAS

### Agents and MAS

- Fulfills all 3 criteria?
  - It is an agent!
- Interacts with other agents?
  - It is a MAS
- Improves performance over time?
  - It is a learning agent



Multiagent Systems and Agent-based Modeling and Simulation

Introduction to AA & MAS

The Basics of AA and MAS

#### In Short

- Agents are
  - Autonomous
  - Flexible
  - Have own control
  - Interact (with other autonomous agents)
  - Are situated (in an environment)



The Basics of AA and MAS

#### Environment

- Environment = sensing (perception) + action
- Types of environment:
  - Totally vs. partially observable
  - Deterministic vs. non-deterministic
  - Episodic vs. non-episodic (sequential)
  - Discrete vs. continuous
  - Static vs. dynamic
  - Single agent vs. multiagent



Monoagent vs. Multiagent Al

## Monoagent Al

- Revisiting some basics of (mono or single agent) AI
- Relevant areas to discuss role of multiagent
  - Planning and decision making
  - Learning
  - Problem solving via constraints satisfaction/optimization



- Planning task: find a sequence of actions to reach a given goal
- How to go from Berlin to Coimbra to present a tutorial?
  - agent that plans: look for routes, timetables, etc. and plans
  - assumes an initial state and a goal
  - another way is...



Monoagent vs. Multiagent Al

- Agent as utility maximizer (via MDP - Markov decision processes)
  - Set of states S
  - Set of actions A
  - transitions
  - $S \times A \rightarrow \mathbb{R}$
- Able to deal with uncertainty



Monoagent vs. Multiagent Al

- Agent as utility maximizer
  - In principle:
    - possible to model any decision process of the agent via an MDP
  - In practice:
    - Some limitations (see later)



Monoagent vs. Multiagent Al

- This works fine for ONE agent...
- ... but: how about more than one?



### Monoagent AI - Learning

- Learning
  - Important role in any system that intends to be intelligent
  - Set of algorithms that increase the ability of the agent to match a series of inputs to their corresponding outputs
- Important here:
  - Reinforcement learning (RL)
    - We do not tell the agent explicitly what to do or which action to make
    - Agent has to select the action that achieves the highest reward (initially by trial and error)



Monoagent vs. Multiagent Al

#### Monoagent AI - Learning

- This works fine for ONE agent...
- ... but: how about more than one?



Monoagent vs. Multiagent Al

## Monoagent AI – Problem solving with CSP

- One approach to problem solving
  - Constraint satisfaction problem (CSP)
    - Set of variables
    - Set of constraints
    - Solution: assignment of values for each variable so that no constraint is violated



### Monoagent AI - Problem solving with CSP

- CSPs may have no solution or have several solutions
- Thus: constraint optimization problem (COP)
  - Find the best solution
    - Quality criteria to evaluate each solution
    - Cost function



Monoagent vs. Multiagent Al

### Monoagent AI - Problem solving with CSP

- This works fine for ONE agent...
- ... but: how about more than one?



Monoagent vs. Multiagent Al

### Multiagent Al

- One vs. several agents:
  - Partial, local knowledge about the problem
  - ...
- How efficient are classical techniques?
- After all.... what changes?
- We will see this in details by revisiting each of those 3 areas



Multiagent Systems

#### **Definitions**

- Definition of MAS: again, no definitive definition
- Def. 1:

   a multiagent system is a system composed by several agents that interact
- Def. 2:
   A multiagent system is one that consists of a number of agents, which interact with one another. To successfully interact, they will require the ability to cooperate, coordinate, and negotiate with each other, much as people do. (Wooldridge)
- Multiagent systems and collective intelligence are not the same

Multiagent Systems and Agent-based Modeling and Simulation

Introduction to AA & MAS

└ Multiagent Systems





Multiagent Systems

- 1906 / UK: F. Galton visits an agricultural exposition
- Hundreds of "non experts" bet about the weight of an ox (which participates in the exposition)
- Galton believes that only experts (e.g., breeders) can correctly evaluate the weight
- But: the average weight comes out correctly !!!



└- Multiagent Systems

- 1987 / Challenger explosion:
- Financial market "knew", half an hour after the accident, that the Thiokol company was responsible (Thiokol shares went down 12% that day, while shares of other suppliers went down only 3%)
- This did not appear in the press
- Technical committee in charge: report after 6 months charging Thiokol



Multiagent Systems

- Iowa Electronic Markets (IEM): forecast elections results
  - 1998–2000: error of just 1.37% in the Bush vs. Al Gore presidential election; 3.43% in other American elections; 2.12% foreigner elections
  - Performance superior to opinion polls
  - Hollywood Stock Exchange (HSX): box office, Oscar, etc.



Multiagent Systems

- 4 conditions for a wise collective:
  - diversity of opinions (each person must have private information, even if only an eccentric interpretation of the facts)
  - independence (individuals opinions are not determined by others' opinions)
  - decentralization (individuals deduce from local knowledge)
  - 4 aggregation (mechanism to aggregate the responses)



└ Multiagent Systems

### Collective Intelligence

#### Surowiecki:

If a group satisfies those conditions, its judgment is likely to be accurate. Why? The answer lies on a mathematical truism. If you ask a large enough group of diverse, independent people to make a prediction, and then average those estimates, the errors each of them makes in coming up with an answer will cancel themselves out. Each person's guess has two components: information and error. Subtract the error and you're left with the information.



Multiagent Systems

- Not so easy case: when an individual decision depends on the collective
- This is the case in the number game and all games of the minority game class
- Let us now play one instance of this game...



- Introduction to AA & MAS
  - Multiagent Systems

### Minority/Majority Games

- Pick one of the 3 objects
- Winner(s) is/are whoever picks the most picked object (i.e., is in the majority)







object B



object C



└ Multiagent Systems

# Minority/Majority Games

- If you and m other participants have to select / pick the
  most beautiful (or any other quality) among n objects, and
  giving that those selecting the most (or least) selected one
  win the game, the best strategy is not to select the object
  that you prefer, but rather the one which you think is the
  most preferable
- If everybody does this reasoning, the elected object may be neither the one you prefer, nor the one that the majority prefers
- people usually achieve a "third degree of anticipation", i.e., they anticipate what the majority of people would select and react accordingly

-Introduction to AA & MAS

Multiagent Systems

# Minority/Majority Games

- Minority / Majority games are common in the real world:
  - free search engine (what is the point in using a search engine nobody uses?)
  - 2 same goes for fax machines
  - oute choice
  - 4 technological standards (e.g., betamax vs. VHS or blueray vs. DVD)



Introduction to AA & MAS
Multiagent Systems

#### In Short

- MAS are not only about collective intelligence (in fact it seldom is)
- It is much more about coordination of decisions made by autonomous, deliberative agents that share an environment



# Elements of a MAS

- <u>Environment E</u> (in general, a *n*-dimensional space where all interactions among agents are represented)
- Set of passive objects O situated in the space, which can be perceived and modified by the agent
- Set A ( $A \in O$ ) of situated agents, i.e., at each given time, each agent is positioned in the space
- Set R of relations between the objects and the agents
- Set O<sub>p</sub> of operations with which the agents perceive, produce, consume, transform, or manipulate the objects
- Set O<sub>e</sub> of operations over the environment, which represent the effects of Op in the world, and the reactions over the agents and objects (universal laws)

# MAS: Classification

- Number of agents: fix or open
- Granularity: agents described according to their expertise or behavior
- Heterogeneity: one or various classes of agents?
- Organization: from hierarchical to flat societies
- Cooperation or antagonism
- Complexity of interactions: explicitly or implicit communication
- Coupling: intensity of the interactions (can be measured by the relationship between communication acts and inference quantity)

Introduction to AA & MAS

Multiagent Systems

#### MAS: Associated Concepts

- Organization
- Interaction
- Coordination
- Cooperation
- Communication



Introduction to AA & MAS

Multiagent Systems

#### Interactions

- Agent Agent
  - Caused by actions or series of actions that have any effect over the agents' behavior
  - Example: 2 agents wish to occupy the same place (in the space) at the same time
- Agent Environment
  - Dynamic environment can be a problem for the agent



Multiagent Systems

#### Interactions

- Types:
  - Via explicit communication
  - Indirect by means of the environment (agent observes a change in the environment)
- Effect: changes in the environment state, as well as in other agents
- Cooperation or antagonism has an important role
- Pre-condition for occurrence:
  - Agents that communicate (explicitly or implicitly) and/or negotiate
  - Agents shall have motivation to interact (e.g., common (sub)goal, use of same resource) or meet physically (e.g., possible collision between robots)

# Types of Interaction: Classification

- Regarding goals:
  - Compatible
  - Incompatible:
    - agent A's goal is to reach state p, and B's goal is to reach state q
    - if  $p \rightarrow \neg q$  then: Goal (A, p)  $\rightarrow \neg$  reachable (Goal(B, q))
- Implication:
  - (potentially) cooperative situation when goals are compatible
  - Antagonist when the goals are incompatible



# Types of Interaction: Classification

- Regarding task type:
  - Simple: can be individually carried out
  - Complex: can be better carried out if in a joint way
  - Those that can only be carried out jointly (via cooperation)
- Regarding resource:
  - Sufficient
  - Insufficient



Multiagent Systems and Agent-based Modeling and Simulation

Introduction to AA & MAS

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#### Coordination

 Act of manage dependencies among activities (Malone and Crowston, 1994)



└ Multiagent Systems

#### Communication

- Necessary for coordination and cooperation
  - Explicit (speech acts, language, protocols)
  - Implicit (game theory, pheromone, etc.)



Multiagent Systems

# Cooperation in MASs

- Individuals have limited abilities and knowledge about the environment and its dynamics
- Resources are not limited
- Improves the performance
- Reduces redundancy
- Conflict handling
- Agents' plans may hinder or damage other agents' plans
- Agents' plans may help or make possible other agents' plans



Introduction to AA & MAS

Multiagent Systems

#### MASs: Main Messages

- Ideally: try to replicate collective intelligence
- Global behavior emerging from local behavior (and perceptions)
- Representation of a MAS: tuple
- Choice of sensors, type of communication: important questions



Introduction to AA & MAS
Multiagent Systems

#### Overview

- We will revisit these 3 areas in the light of what we know from MASs:
  - Planning and decision making using MDP
  - Learning
  - Problem solving via constraints satisfaction/optimization
  - (We start by looking at the respective single agent case and then revisit to check what changes in multiagent cases)
- But (before) we now introduce agent-based modeling and simulation (where we can use concepts from MASs)...



#### **ABMS: General Concept**

- ABMS: MASs in a simulated environment and in virtual time
- Concept is based on MASs:
  - Entities = Agents
  - Environment composed of:
    - other agents and
    - other environmental entities such as objects, resources
  - Interactions among agents are key
  - ABMS = agents + environment + interactions



# Granularity of Representation of the Elements of the System

- Determining the level of detail to be used
- Two basic forms
  - Macrosimulation: system perspective
  - Microsimulation: fine grained entities with distinct state and behaviour
- Also possible: mesoscopic models



#### Why ABMS?

- New paradigm that allows more appropriate modelling in:
  - Social science
  - Biology
  - Traffic
  - Other socio-technical systems
  - Emergent phenomena
  - ...
- Provides a more intuitive way of modelling (closer to the real system) thus facilitating the task of non-experts



#### Relation to Cellular Automata

- CAs: Discrete in space and time
- Spatial locality plays key role
- Uniform rules assigned to cells
- Next state of cell is computed exclusively based on its last state and on the states of neighbors
- Two possibilities
  - Agent = cell
  - Agent = state of cell
- Often: CA as basis for environment of agents



#### Advantages

- Agent-based Models are a powerful paradigm:
  - Dealing with real MASs directly: real Agent = simulated Agent
  - Allows modelling of adaptation and evolution
  - Modelling of heterogeneous space and population
  - Different levels of observation



#### Developing an ABMS

- Top down approach:
  - Related to agent-oriented software engineering (AOSE)
  - Takes into account existing/known organizational structures
  - Focus on the phenomena (described on a global level): start describing the phenomena and later derive agents/behaviors



#### Developing an ABMS (cont.)

- Bottom up approach:
  - Focus on agents: observing real-world agents in order to derive simulated agents
  - A global behavior may emerge
  - Trial and error
  - Parameter calibration costly
  - Normally requires much more data



#### Frameworks / Tools

- Netlogo
- Repast
- Swarm
- SeSAm
- MASON
- ..



#### Overview

- We now revisit these 3 areas in the light of what we know from MASs:
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  - Learning
  - Problem solving via constraints satisfaction/optimization
  - (We start by looking at the respective single agent case and then revisit to check what changes in multiagent cases)



Planning and MDP

Sequential Planning and Decision Making for One Agent: MDP

#### MDP: Introduction

- Generalization of search and planning problems
- Method to decide what to do today, given that we will decide again tomorrow
- Sequential decision problems where the utility of each agent depends on a sequence of decisions (MDP) and/or on the decision of various agents (MMDP), eventually under partial observation (POMDP)
- Markov assumption: the effects of an action taken in a given state depend only on this state (not on the past history)



Planning and MDP

Sequential Planning and Decision Making for One Agent: MDP

#### Related Concept: discounted reward

- discounted utility /reward / payoff:
  - what is preferable? 90 dollars now or 100 in one month?
  - 90 now > 100 later ???



# Related Concept: discounted reward (cont.)

- Future payment does not worth the same as payment now (uncertainty regarding being paid, inflation, etc.)
- assuming a discount rate of 0.9, 100 is worth only 90 in the next month!
- Salary of 1000 per month  $\neq$  1000 + 1000 + 1000 + ...  $\rightarrow \infty$
- We cannot say now that your salary is infinite!
- Devaluation is given by (0.9)<sup>N</sup>
- Discount rate  $\gamma$ :
  - total salary: (salary now) +  $\gamma \times$  (next month salary) +  $\gamma^2 \times$  (salary in 2 months) +  $\gamma^3 \times$  (salary in 3 months) + ...



# Example 1: Academic Life

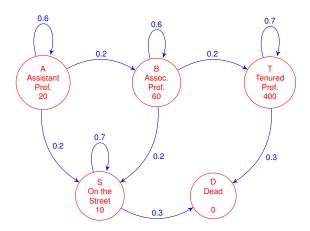
- Here: only state transitions
- Be:
  - *V*: value of expected future discounted reward
  - $V_A$ ,  $V_B$ ,  $V_D$ ,  $V_S$ ,  $V_T$  same in states A, B, D, S, and T
  - $\gamma = 0.9$
- And an automata that considers these states and transitions between them (e.g., assistant professor to associate professor)
- How to compute the future rewards of academic life???



Planning and MDP

Sequential Planning and Decision Making for One Agent: MDP

#### Example 1: Academic Life





Planning and MDP

Sequential Planning and Decision Making for One Agent: MDP

#### **MDP**

- Formally defined by:
  - set of states  $S = \{s_1, s_2, ..., s_n\}$
  - set of actions  $A = \{a_1, a_2, ..., a_n\}$
  - probability or state transition matrix P where  $p_{ij}$  = prob. (next state= j | current state = i)
    - obs.: in general, also considers the action taken
  - rewards for each state  $R = \{r_1, r_2, ..., r_n\}$
  - discount factor  $0 < \gamma \le 1$
- For each step i:
  - state  $s_i$ , action  $a_i$ , reward  $r_i$
  - $\bullet$  random transition to the next state  $(s_j)$
  - $\bullet\,$  all future rewards are discounted by  $\gamma\,$



#### **Exact Solution for MDP**

- $V^*(s_i)$  is the expected value of the future discounted sum of rewards from state  $s_i$  (also denoted as utility or  $U(s_i)$ )
- $V^*(s_i) = r_i + \gamma [p_{i1} V^*(s_1) + p_{i2} V^*(s_2) + \ldots + p_{in} V^*(s_n)]$

Be

$$V = \begin{bmatrix} V^{\star}(s_1) \\ \vdots \\ V^{\star}(s_n) \end{bmatrix} \quad R = \begin{bmatrix} r_1 \\ \vdots \\ r_n \end{bmatrix} \quad P = \begin{bmatrix} p_{11} & p_{12} & \dots & p_{1n} \\ \vdots & \ddots & & \\ p_{n1} & p_{n2} & \dots & p_{nn} \end{bmatrix}$$

- $V = R + \gamma [P \times V]$
- Good news: exact solution!
- Bad news: for  $10^2$  states, it is necessary to solve a  $10^2 \times 10^2$  system of equations!



# Policy and Optimal Policy for an MDP

- Policy: mapping from states to actions (i.e., what exactly the agent should do in each state that is reachable from a given state)
- $\Pi(s_i)$  is the policy for state  $s_i$
- Quality of a policy: given by the expected utility
- Optimal policy  $\Pi^*(s_i)$ : policy that yields the highest expected utility (there is no better option than follow  $\Pi^*$ )
- For each MDP there exists an optimal policy (how to compute it?)
- Policies can be expressed as tables (but this is not efficient)



Planning and MDP

Sequential Planning and Decision Making for One Agent: MDP

# Computing the Optimal Policy

- Enumeration and choice: not feasible in real-world problems
- Thus: dynamic programming
- Case 1: finite horizon (fix time *k*)
  - with a finite horizon, the optimal action can change with time (non-stationarity)
- Case 2: infinite horizon
  - if there is no time limit, then there is no reason to behave in a different manner if the agent is in the same state in different time steps
- Example Powerball Lottery: if you know that the Powerball Lottery will no longer exist from tomorrow on, how do you act? and if it will end in 10 days? in 100? and in case you do not have this information (assuming that the Powerball Lottery will be there forever)?

# Computing the Optimal Policy (cont.)

- Computing policies for infinite horizon is simpler (due to the stationary nature)
- In infinite horizon, by using discounted rewards, the utility of an infinite sequence of actions is finite
- When  $\gamma$  < 1, we have

$$V[s_0, s_1, ...] = \sum_{t=0}^{\infty} \gamma^t R(s_{i,t}) \le \sum_{t=0}^{\infty} \gamma^t R_{max} = \frac{R_{max}}{(1-\gamma)}$$
 (geometric series)

•  $\Pi^* = \arg\max_{\Pi} \mathsf{E} \left[ \sum_{t=0}^{\infty} \gamma^t R(s_{i,t}) \middle| \Pi \right]$  where E is the expected value



# Bellman Equations (1957)

- Be  $V^k(s_i)$  the maximum sum of the discounted future reward from state  $s_i$  at time step k, if agent chooses action a
- $V^0(s_i) = r_i$
- In each time step N + 1:

$$V^{N+1}(s_i) = \max_{a} \left[ r_i + \gamma \sum_{j=1}^n p_{ij}^a V^N(s_j) \right]$$

- one equation for each state!
- The expected utilities of the sequence of states (V[s<sub>0</sub>, s<sub>1</sub>, ...]) are the unique solution of the set of Bellman equations



Planning and MDP

Sequential Planning and Decision Making for One Agent: MDP

# Steps for Solving Bellman Equations

- Solve |S| simultaneous equations
- Equations are non linear
- Hard to solve analytically; thus iterative solution:
  - $\bullet$  initialize  $V^0$  with arbitrary values
  - ② for each S, compute V(S) from R(S) and  $V^0(S)$
  - use these new utility values to update V
  - 4 repeat steps 2 and 3 until V converges
- This equilibrium is the unique solution



# Solving MDP via Value Iteration

- compute  $V^1(s_i)$  for each i
- compute  $V^2(s_i)$  for each i
- •
- $V^k(s_i)$  for each i
- •
- ... until convergence!
- when?
  - when  $\max_{i} |V^{N+1}(s_i) V^N(s_i)| \le \epsilon$



# Value Iteration: Algorithm

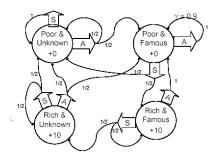
```
function value iteration(S,P,R,\gamma,\epsilon)
repeat
    V[] \leftarrow R[]; \delta \leftarrow 0
   for each state s \in S do
       do V'[s] \leftarrow R[s] + \gamma \max_{a} \sum_{s'} p_{ij,a} V[s']
       if |V'[s] - V[s]| > \delta then
          \delta \leftarrow |V'[s] - V[s]|
       end if
   end for
until \delta < \varepsilon \times \frac{1-\gamma}{\gamma}
output V
```



Sequential Planning and Decision Making for One Agent: MDP

### **Example with Actions**

- you are the owner of a company
- actions at each time step: invest (S) or advertise your product (A)
- be the states and transitions graph





Sequential Planning and Decision Making for One Agent: MDP

### Example with Actions (cont.)

• applying the algorithm (with  $\gamma = 0.9$ ):

k	$V^k(PU)$	$V^k(PF)$	$V^k(RU)$	$V^k(RF)$
0	0	0	+10	+10
1	0	4.5 <sup>(1)</sup>	14.5	19
2	2.03	$8.55^{(2)}$	16.53	25.08
3	4.76	12.2 <sup>(3)</sup>		
:				

3 
$$V^3(PF) = R(PF) + \gamma \times max \left\{ \frac{2.03}{2} + \frac{25.08}{2}, 8.55 \right\} = 12.2$$



Sequential Planning and Decision Making for One Agent: MDP

### Sequential Decision Problems

- MDP's involve two main questions
  - is horizon finite or infinite?
    - how to find the optimal behavior?
      - value iteration
      - policy iteration Involve two main questions



Sequential Planning and Decision Making for One Agent: MDP

### Horizon

- Question 1, finite horizon:
  - there is a fixed time *n* after which the interaction with the environment ends
  - formally:  $U([s_0, s_1, ..., s_{n+k}]) = U([s_0, s_1, ..., s_n]), \forall_{k>0}$



Sequential Planning and Decision Making for One Agent: MDP

### Horizon (cont.)

- Question 1, infinite horizon:
  - with no fixed time limit
  - there is no reason to behave differently in a given state at different times
  - optimal behavior depends only on the current state
  - optimal policy is stationary
  - simpler case



Sequential Planning and Decision Making for One Agent: MDP

# **Optimal Behavior**

- Question 2: How to find the optimal behavior?
  - an option: list all behaviors and choose the one(s) with the highest possible value for each initial state
    - not feasible!
  - better option: calculate value functions
    - compute the so-called optimal value function and then the optimal behavior
    - the optimal value of the state s, V\*(s), is the one that obtains the highest expected value when the agent starts in state s
    - this means: compute the utility itself (U or V) and, with this, the optimal behavior



Sequential Planning and Decision Making for One Agent: MDP

#### **POMDP**

- Relaxation of the hypothesis "environment is completely observable"
  - agent does not necessarily know what state it is in
  - how to execute the recommended policy for the state it is in?
  - state utility s and optimal action in s depend not only on s but also on how much the agent knows when it is in s
- POMDP is more difficult than MDP
- POMDP is more realistic than MDP



Sequential Decision Making in MASs: MMDP / SG

# Multiagent MDP

- An agent trying to decide sequentially while other agents are in the environment trying to do the same
- MDP for more than one agent is a multiagent MDP (MMDP), also known as (stochastic game or SG)
- Base: game theory!



### Stochastic Games

- A stochastic game (SG) is defined by a set of states **S** with a stage game defined for each state  $s \in S$
- In each state s, player i can choose actions from set  $\mathbf{A}_i(s)$
- One of the stage games is played at each time t = 0, 1, 2, ...
- The actions played by the players determine not only their immediate rewards (payoffs), but also the probability of transitioning to any given state a the next time step
- This means: given that 2 players 1 and 2 are in state s and choose actions  $a_1 \in \mathbf{A}_1$  and  $a_2 \in \mathbf{A}_2$ , these players receive rewards  $r_1(s, a_1, a_2)$  and  $r_2(s, a_1, a_2)$ ; also, the probability they find themselves in state s' in the next time step is  $p(s'|s, a_1, a_2)$

Sequential Decision Making in MASs: MMDP / SG

# Stochastic Games (cont.)

 Definition: a strategy is called a Markov strategy if the behavior of a player at time t depends only on the state s; a pure Markov strategy specifies an action a(s) for each state s ∈ S



Sequential Decision Making in MASs: MMDP / SG

### Stochastic Games (cont.)

- Henceforth the following assumptions are made:
  - the length of the game is not know to the players (i.e., the horizon is infinite)
  - 2 rewards and transitions are time-independent
  - strategies are Markov



# Multiagent MDP

- Generalization of an MDP for n agents is given by the tuple MMDP=  $(\mathcal{I}, \mathbf{S}, \mathbf{A}, \mathcal{P}, \mathcal{R})$ 
  - set of agents  $\mathcal{I} = 1..., i, ..., n$
  - set of states S
  - set of actions A
  - ullet reward function  ${\cal R}$
  - ullet transition probability matrix  ${\cal P}$
- Also (depending on the modeling):
  - $\mathbf{A} = \times_{i \in \mathcal{I}} A^i$  and  $\mathbf{S} = \times_{i \in \mathcal{I}} S^i$
- Depending on the actions performed by the agents, a transition occurs that determines a new state, i.e. a new reward matrix
- We already know the rest (from the theory of repeated games)



Multiagent Systems and Agent-based Modeling and Simulation

Planning and MDP

Sequential Decision Making in MASs: MMDP / SG

### MDP and GT

(1 agt ?, 1 tmstep ?, fully obsv. ?)

NFG (F,T,T)



Multiagent Systems and Agent-based Modeling and Simulation

Planning and MDP

Sequential Decision Making in MASs: MMDP / SG

### MDP and GT

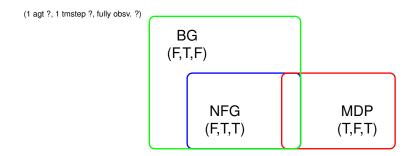
(1 agt ?, 1 tmstep ?, fully obsv. ?)

NFG (F,T,T) MDP (T,F,T)



Sequential Decision Making in MASs: MMDP / SG

### MDP and GT

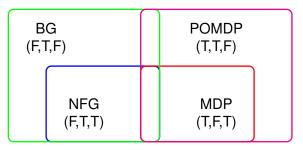




Sequential Decision Making in MASs: MMDP / SG

#### MDP and GT

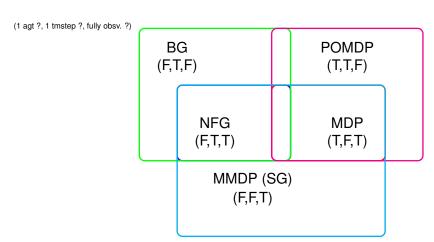
(1 agt ?, 1 tmstep ?, fully obsv. ?)





Sequential Decision Making in MASs: MMDP / SG

#### MDP and GT



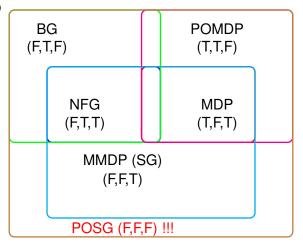


Sequential Decision Making in MASs: MMDP / SG

### MDP and GT

(1 agt ?, 1 tmstep ?,

fully obsv. ?)





# MDP & POMDP: Suggested Reading

- Givan, Bob. MDP Tutorial definitions and extensions, Dagstuhl, November, 2001
- Jensen, PA and Bard, JF. Operations Research: Models and Methods. John Wiley & Sons, NJ, 2003
- Muñoz-Avila, H. Uncertainty and Utility (for Lehigh University CSE 395/495 Spring 2003)
- Russell, SJ and Norvig, P. Artificial Intelligence: a Modern Approach. Prentice Hall, NJ, 2003 (2nd ed.)
- Leslie Pack Kaelbling, Michael L. Littman and Anthony R. Cassandra. Planning and Acting in Partially Observable Stochastic Domains. Artificial Intelligence, Vol. 101, 1998.
- Goldman, C.V. and Zilberstein, S. (2004). Decentralized Control of Cooperative Systems: Categorization and Complexity Analysis, Volume 22, pages 143-174.



Reinforcement Learning

#### Overview

- We now revisit these 3 areas in the light of what we know from MASs:
  - Planning and decision making using MDP
  - Learning
  - Problem solving via constraints satisfaction/optimization
  - (We start by looking at the respective single agent case and then revisit to check what changes in multiagent cases)



Basics

### Machine Learning

- Numerous methodologies
  - symbolic, connectionist, etc.
  - tree induction
  - genetic algorithms and evolutionary computation
  - neural networks
- None is directly linked to decision
- (and also not to autonomy)
  - How to act?
  - What action to take in each situation?



# Machine Learning

- We have already seen how planning in nondeterministic environments (i.e., with uncertainty) can be realized by calculating and using optimal policies
  - this assumes that the agent has (knows) the correct model of the environment (i.e. knows P and R)
- Now we will see that an agent who does not know such a model can learn about this
  - how? interacting with the environment!



L<sub>Basics</sub>

### Motivation for RL

- Given a goal to be achieved by the agent:
  - we do not want to have to detail, step by step, how the agent should act
  - we want the agent to find out how to act in each situation
  - Autonomy
- What information do we give to the agent?
  - We do not tell the agent if its decision is right or wrong
  - Rather: we give only an indication about the instant quality for each decision → a reward sign



L<sub>Basics</sub>

### Motivation for RL (cont.)

- Learning by reinforcement
  - Can not be considered supervised or unsupervised learning
  - Can be imagined as learning with a critic
- Initially inspired by the experiments of psychology
- Classic conditioning (Pavlov's dogs)
- Law of effect (Thorndike / Skinner)
  - Stimulus-reinforcement associations (positive or negative)
  - Positive reinforcements strengthen the probability of a behavior
  - Negatives reinforcements weaken such probability



### Motivation

- Algorithms for reinforcement learning
  - Given a world description, agent learns how to act optimally
    - list of possible actions
    - quality indication of each action in each situation → sign of reward for each action in each state
  - We allow the agent to practice and learn (trial-and-error)!



- How do we formalize this? Markov models
  - generalization of search and planning problems
  - methods for deciding what to do now, given that after we will decide again
  - sequential decision problems (MDP, MMDP, POMDP ...)
  - Markov hypothesis: effects of an action taken in a given state depends only on this state and not on past history



Reinforcement Learning

Single-agent RL

- Markov models
  - set of states S;
  - set of actions A;
  - set of "preferences", or reinforcement signs
    - tell the agent how good (or bad) each action is, in each situation where it can be applied
    - $R: \mathcal{S} \times \mathcal{A} \rightarrow \Re$ ;
  - probabilistic transition function  $T : S \times A \rightarrow \Pi(S)$ 
    - T(s, a, s') = transition probability  $s \rightarrow s'$  given action a



Reinforcement Learning

Single-agent RL

### Formalization as MDP

#### Example 1:

- Environment: You are in state A and have 4 possible actions
- Agent: I choose action 2
- Environment: You received reinforcement sign of +7
  points. You are in state B and have 5 possible actions
- Agent: I choose action 5
- Environment: You received reinforcement sign of -2 points. You are in state F and have 2 possible actions
- Agent: I choose action 2
- Environment: you are in state A and have 4 possible actions
- Agent: I choose action 2
- Environment: You received reinforcement sign of +7
- ...



- Example 2:
  - Environment: You are in state A and have 4 possible actions
  - Agent: I choose action 2
  - Environment: You received reinforcement sign of +7
    points. You are in state B and have 5 possible actions
  - Agent: I choose action 5
  - Environment: You received reinforcement sign of -2 points. You are in state F and have 2 possible actions
  - Agent: I choose action 2
  - Environment: you are in state A and have 4 possible actions
  - Agent: I choose action 2
  - Environment: You received reinforcement sign of +1
    points. You are in state C and have 3 possible actions





- Goal: find an optimal policy  $\pi^*$ 
  - for every possible state s: indicates which is the best action
  - this means:  $\pi(s) = a$
  - what does "best action" mean?
    - leads the agent to states from which it can earn more "points" (signs) of reinforcement
    - .. (assuming the agent continues to act as best it can)
  - reinforcement points the agent will get in the future are the expected ones
    - transitions are probabilistic
    - worse: reinforcement may not be deterministic !!! (What is the difference between previous examples 1 and 2?)



- How to measure how good is each situation in which the agent can be?
- We associate each state s with a value V(s)
  - V = reinforcement that we hope the agent will receive in the future
  - given that the agent starts in s and continues selecting optimal actions
- We have already seen how to compute optimal policies (value iteration, policy iteration)



### **Problems**

- Problem with policy iteration and value iteration:
- Agent needs to know several things
  - T(s, a) (or P), for all s and all a
  - R(s, a), for all s and all a
  - in other words, agent needs to know the environment model
  - the agent should not need to know everything about his environment, before it can act (babies!)
- Can we estimate V(s) without having the model?



### **RL Types**

According to the type of agent design, a type of learning

agent design	know	learn	use
utility-based	T	R  o U	U
Q-learning-based	-	Q(s,a)	Q
reflex agent	-	$\pi$	$\pi$

- Besides this, passive or active learning:
  - passive: agent follows the prescribed policy and only explores if, due to the stochasticity in the environment, it visits a certain state "by accident"
  - active: agent greedy uses the prescribed policy (as in the passive) but exploits other alternatives with a low probabili

- Reinforcement Learning
  - Single-agent RL

### Q-Learning

- Almost the same thing as calculating V, but ...
  - instead of calculating a V value for each **state** 
    - i.e. "how good it is to be in this state"
  - calculates a value Q(s, a), for each s and each a
    - i.e. "how good is to perform this action in this state "
  - the agent perceives its state s, chooses an action a and receives a reward r
  - ullet .. then updates its estimate of Q value for the pair < s, a >

• 
$$Q(s, a) = (1 - \alpha)Q(s, a) + \alpha \left(r + \gamma \max_{a'} Q(s', a')\right)$$



- Reinforcement Learning
  - Single-agent RL

### Q-Learning

- And how does the agent choose an action?
- If it is in s and there it can do 4 actions:
  - has estimates for how good it is to perform each of these actions
    - $Q(s, a_1), Q(s, a_2), Q(s, a_3)$  and  $Q(s, a_4)$
- It chooses the largest!
- $\pi(s) = argmax_aQ(s, a)$
- Direct relationship of Q with V:  $V^*(s) = \max_{a} Q^*(s, a)$



Single-agent RL

### Q-Learning

- Shall the agent always choose the best action?
  - No! because it would then not explore further!
- There are several ways to balance exploration and exploitation (of the best perceived action): known as exploration-exploitation dilemma
  - epsilon-greedy: select the best action (greedy action selection) most of the time but, with a small probability  $(\varepsilon)$  select a random action
  - other methods such as softmax / Boltzmann exploration



Single-agent RL

#### **Problems**

- Reinforcement learning has several problems
  - non-stationary environments
    - agent "forgets" already computed policies (only the last one is saved)
    - solution: multiple models, one for each "state" of the environment
  - non fully observable environments
    - the agent is not sure which is the current state
    - solution: POMDP, etc. (based on beliefs)
  - exponential number of states or combination of states—actions
    - solution 1: state abstraction
    - solution 2: hierarchical reinforcement learning



# Multiagent reinforcement learning

 Agent tries to solve a problem / tries to learn while other agents are in the environment trying to solve their learning problems (related or not)



- Problems with MARL (multiagent RL)
  - Fundamental hypotheses of RL are violated
  - Interaction in dynamic environment (dynamics come from other agents reacting to the same environment)



- Formalization as MMDP / SG:
  - There is no known general solution (e.g. general sum games)
  - Combinatorial explosion on states and actions
    - Set of states  $S_1 \times S_2 \times \cdots \times S_n$
    - Set of actions  $A_1 \times A_2 \times \cdots \times A_n$
    - $S_1 \times S_2 \times \cdots \times S_n \times A_1 \times A_2 \times \cdots \times A_n \rightarrow \Re$
    - It is necessary to visit an exponential number of combinations of pairs S, A



└- Multiagent RL

- Some ways to deal with the aforementioned problems:
  - Ignores the presence of other agents learning and applies simple RL
  - Perceives the presence of other agents but seeks an independent convergence
  - Adapts to the other agents seeking the optimality
  - Agents can be heterogeneous ...



- A first idea is for each agent to learn ignoring the others
- Agent uses Q-Learning as if it were unique in the environment
  - Treats other agents as part of the environment
  - It works if the behavior of the other agents is fixed
  - If other agents also learn, agent policy i has to adapt to the adaptation of others
  - This is why multiagent RL is so hard



Reinforcement Learning

└-Multiagent RL

- Types:
  - Cooperatives / team game:  $\rho_1 = \rho_2 = ... = \rho_n$
  - Competitive / zero-sum game:  $\rho_1$  =  $\rho_2$
  - Competitive / non-zero-sum game: more general case



- Reinforcement Learning

Multiagent RL

- Purely cooperative:
  - Global state: includes states of all agents
  - Set of actions that considers all agents
  - Value Q(s, a) would be  $Q(< s_1, s_2, ... s_n >, < a_1, a_2, ..., a_n >)$
  - Problem: Q Table too big and the communication should be unrestricted!



- Example of Q table explosion:
  - *n* agents, *m* actions each and *k* states  $\rightarrow m^n * k$  entries in Q table
  - simple problem: consider 3 agents in a grid of size 10x10 cells, with 4 possible actions (move to: up, down, right, left)  $\rightarrow 4^3 * 100^3 = 64$  million entries in Q table!





- Alternatives to full description:
  - share information (perceptions, policies or episodes)
  - sparse Q table
  - unification of similar states (using function approximation)



# Sparse and Cooperative Q-learning

- Hypothesis: in several problems agents need to coordinate their actions in only a few states, while in others they can act independently
- Idea: groups of agents learn how to solve a task in a cooperative way when the coordination requirements are known beforehand
- Details: Oliveira and Bazzan (2009); Bianchi and Bazzan (2012)



- Seen by the Game Theory ...
  - a joint strategy is Pareto-optimal if there is no strategy that increases payoffs of all agents / players
  - a strategy x<sub>i</sub> of an agent is dominant if it is always the best, regardless of the action of the other agents
  - x<sub>i</sub> is the best answer to x<sub>-i</sub> if is maximizes the payoff



- Seen by Game Theory ... (continued)
  - a joint strategy x is an equilibrium if the strategy of each agent is simultaneously the best response to the strategy of the others
  - that is, there is no incentive to deviate: Nash equilibrium
  - at least one Nash equilibrium always exists but several may exist and / or be difficult to calculate ...



- Single-agent systems (with MDPs): there is always a deterministic optimal policy
- Multi-agent systems (with MDPs): deterministic policies can be dominated (not interesting)
- How to define an optimality criterion?
  - Agent performance according to strategies of other adaptive agents
  - Nash equilibrium



# Recurring discussion on MARL

- Criticism of Shoham et al (Stanford):
   If multiagent learning is the answer, what is the Question?
- Answer from Peter Stone (University of Texas)
   Multiagent learning is not the answer. It is the Question.
- See Al Journal 171(7), 2007



#### Remarks on MARL

- Multiagent learning models / algorithms consider small scenarios with 2 agents
- Almost always when there are more than 2 agents, these are completely homogeneous
- How to reduce state space?
- Open problems: co-learning (e.g. heterogeneous agents), nondeterministic environments, large number of agents and / or states ....
- Which techniques could be used together?



# Remarks on MARL (cont.)

- Multiagent scenarios much harder than single agent ones
- Adaptation is key
- Nature inspiration (e.g. self organization for task allocation in the rescue scenario)
- Challenges



# Suggested Reading

- Kaelbling et al., 1996: Reinforcement Learning: A Survey
- Artificial Intelligence Journal (Volume 171, Issue 7, Foundations of Multi-Agent Learning)
  - Yoav Shoham, Rob Powers and Trond Grenager. If multi-agent learning is the answer, what is the question?
  - Peter Stone. Multiagent learning is not the answer. It is the question.
- Sutton and Barto 1998: Reinforcement Learning: An Introduction.

Book available at:

http://www.cs.ualberta.ca/~sutton/book/ebook/the-book.html



#### Overview

- We now revisit these 3 areas in the light of what we know from MASs:
  - Planning and decision making using MDP
  - Learning
  - Problem solving via constraints satisfaction/optimization
  - (We start by looking at the respective single agent case and then revisit to check what changes in multiagent cases)



# **CSP** and Beyond

- We now discuss problem solving using constraint satisfaction...
- ... and extension to the multiagent case
- In the beginning... it was... CSP (constraint satisfaction problem)
  - CSP → COP (constraint optimization problem)
  - CSP → DisCSP (distributed CSP)
  - DisCSP → DCOP (distributed COP)



CSP and COP

# **Problem Solving**

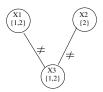
- CSP: based on search algorithms that take advantage of some sort of structure about states of the problem in order to solve it
- A CSP is defined by a set of variables (V<sub>i</sub>) (and their domains) (D<sub>i</sub>), and by a set of constraints
- A solution is an assignment of values to each variable, so that no constraint is violated



# Representation

- It is helpful to represent/visualize a CSP as a constraint graph
- Example: find a value for each variable  $(\{x_1, x_2, x_3\})$  within their domains  $(\{1, 2\}, \{2\}, \{1, 2\})$ , observing the constraints  $(\{\{x_1 \neq x_3\}, \{x_2 \neq x_3\}\})$
- Solution (unique, in this case): assignment

$$\mathcal{A} = \{\langle x_1 = 2 \rangle, \langle x_2 = 2 \rangle, \langle x_3 = 1 \rangle\}$$





CSP and COP

# How about if there is no unique solution?

- some problems have no solution at all (it is not possible to satisfy all constraints)!
  - What can be done here: minimize the number of broken/relaxed constraints, or minimize some cost function
- other set of problems have more than one solution
  - what can be done here: choose the best (in terms of some cost function) among the solutions
- Both these issues contributed to the COP (constraint optimization problems) area where we seek to optimize some cost function



CSP and COP

#### COP

- Find the best solution
- Increases the complexity (optimization rather than satisfaction)
- Formalization of a COP:
  - besides variables, their domains, and constraints
  - for COP:  $\mathcal{F}(A)$ 
    - objective function that maps each solution (set of assignments) to a numerical values
    - normally an aggregation of cost functions f
  - solution: a complete assignment A\* corresponding to a optimal value for the objective function

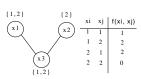


CSP and COP

#### COP

#### Example

- find a value for each variable under the constraints so that the objective function is minimized
- F(A) is given by the sum of various f functions
- $\mathcal{F}(A) = f(x_1, x_3) + f(x_2, x_3)$
- solution: a complete assignment  $A^* = \{\langle x_1 = 2 \rangle, \langle x_2 = 2 \rangle, \langle x_3 = 2 \rangle\}$





L DisCSP and DCOP

# Multiagent AI - DisCSP/DCOP

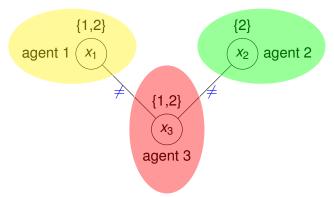
- Distributed Constraint Optimization Problem
  - similar to CSP / COP
    - Instead of centralized: distributed
- Why distributed?
- If centralized:
  - Single point of failure
  - Bottleneck
  - Not possible to centralize all information
    - Network limitation or privacy
- Need to formalize and solve in a distributed way



L DisCSP and DCOP

### Multiagent AI - DisCSP/DCOP

- DisCSP and DCOP
  - Variables and constraints assigned to agents
  - Increased communication





L DisCSP and DCOP

#### DisCSP: Formalization

- m agents 1, 2,..., m
- Each variable  $x_j$  belongs to agent i: belongs $(x_j, i)$
- Constraints are thus distributed among the agents
- Agent I knows constraint  $p_k$ : known $(p_k, I)$
- DisCSP solution:
  - $\forall_i \forall_{x_i}$  where belongs $(x_i, i)$ , the value of  $x_i$  is  $d_i$
  - $\forall_l \forall_{p_k}$  where known $(p_k, I)$  is true,  $p_k$  is true when  $x_j = d_j$



L DisCSP and DCOP

### Distributed Constraint Optimization - DCOP

- Formalization is similar to DisCSP
- But: besides knowing the constraints, agents must also know the cost functions related to these constraints



L DisCSP and DCOP

# DisCSP / DCOP: algorithms

- Agents communicate (via exchanged messages) in order to coordinate and find a solution
- Algorithms
  - DisCSP
    - Asynchronous Backtracking (AB)
  - DCOP
  - Asynchronous Distributed Optimization (Adopt)
  - Distributed PseudooTree Optimization (DPOP)



L DisCSP and DCOP

# BT Algorithm (synchronous)

- Order all agents (some lexicographic ordering)
- 2 The agent with highest priority (e.g.,  $A_1$ ) assigns a value for its variable
- 6  $A_1$  uses a message to send its assignment to the agent with the highest priority after itself (e.g.,  $A_2$ )
- 4 All agents wait for a message containing a partial solution coming from the agent with highest priority below itself
- When A<sub>i</sub> receives a message, it tries to assign a value for its variable, so that no constraint is violated (i.e., all constraints are satisfied)
- **6** If a such assignment is found, then  $A_i$  adds it to the message and sends it to agent  $A_{i+1}$
- If not,  $A_i$  returns the same message (as received) back to  $A_{i-1}$
- $oxed{8}$  A solution is reached when the last agent  $(A_n)$  finds an assignment for its variable
- A non-solution state is declared when the agent with highest priority receives a message back and has no more values to assign to its variable (i.e., the whole domain was already assigned) but no solution was found



L DisCSP and DCOP

# ABT Algorithm (asynchronous)

- Two types of messages:
  - ok? message: this message asks an agent if a given partial solution is acceptable
  - 2 nogood message: this message informs an agent that has sent a partial solution that a constraint violation was found (i.e., the tried value is not good)
- ok? message: higher to lower priority
- nogood message: lower to higher priority



☐ DisCSP and DCOP

# ABT Algorithm (cont.)

- Uses a constraint graph
- Each agent, concurrently, assigns a value to its variable and uses an ok? message to send this value to the agents that are connected to it
- Then the agent waits for an answer
- The agent that has received a nogood message (evaluator agent) keeps a so-called agent\_view (set of values assigned by the agents with which this agent has connection) and have higher priority
- The evaluator agent adds the value received in the ok? message to its agent\_view
- Next, it evaluates whether the assignment for its own variable is consistent with its agent\_view



L DisCSP and DCOP

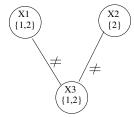
# ABT Algorithm (cont.)

- An assignment is consistent with an agent\_view iff all constraints that are known by the agent remain satisfied when the agent assigns a value to its variable
- If an assignment is not consistent with the agent\_view, then the agent tries to change the value of the variable
- If the agent is unable to find a value that is consistent, then it returns a nogood message



## Example Yokoo

☐ DisCSP and DCOP

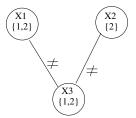


- X1 and X2 send messages with values: (ok? (X1,1)) and (ok? (X2,2))
- X3 creates its agent\_view: (X1,1),(X2,2)
- X3 finds out that this is a nogood
- X3 sends a nogood to X2
- a new link between X2 and X1 is then created (only X2 inserts this new link to its constraint graph)



- Distributed Constraint Optimization
  - DisCSP and DCOP

## Example Yokoo (cont.)

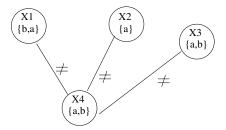


- {(X1,1)} is a nogood because there are no more options of values for X2
- thus X2 sends a nogood message



L DisCSP and DCOP

## Example Bessière



• What if there is no solution?



L DisCSP and DCOP

### Remember: COP

- Finds the best solution
- Increases the complexity (optimization rather than satisfaction)
- Formalization of a COP:
  - besides variables, their domains, and constraints
  - for COP:  $\mathcal{F}(A)$ 
    - objective function that maps each solution (set of assignments) to a numerical values
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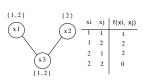


L DisCSP and DCOP

### Remember: COP

### Example

- find a value for each variable under the constraints so that the objective function is minimized
- F(A) is given by the sum of various f functions
- $\mathcal{F}(A) = f(x_1, x_3) + f(x_2, x_3)$
- solution: a complete assignment  $A^* = \{\langle x_1 = 2 \rangle, \langle x_2 = 2 \rangle, \langle x_3 = 2 \rangle\}$





L DisCSP and DCOP

### **DCOP**

- How to do this in a distributed way using agents?
- Popular algorithms: Adopt and DPOP (and their variants)
- Basis:
  - Establish priorities among the agents by means of a search tree (depth search)
  - Nodes in different branches are different sub-problems that can be solved independently (asynchronously)



L DisCSP and DCOP

## DisCSP and DCOP: applications

- Various real world problems which are either inherently distributed or where privacy is an issue:
  - sensor network: choose (assign) a value (e.g. on/off) in a distributed way
  - meeting schedule: choose (assign) a value (e.g. meeting time slot) in a distributed way so that no participant (agent) needs to disclose all information



L DisCSP and DCOP

### DisCSP and DCOP

 Overview methods : Issue 161 – Artificial Intelligence Journal (AIJ)



## The "old days" motivations for multiagent learning

- In MAS: learning helps agents make decisions
- However: now-a-days in the multiagent systems (MASs) community, learning is immediately "translated" into reinforcement learning (RL)
- This is a change in the "old days" motivations for multiagent learning, i.e., interactions between MASs and machine learning (ML) should be manifold



### MASs and ML were closer

- Interactions between MASs and ML should be manifold
- Idea has appeared as early as in the 1990s
  - Brazdil et al. (1991); Brazdil and Muggleton (1991); Davies and Edwards (1995); Sian (1991)
  - European Working Session on Learning (EWSL-91)
- However: we still keep saying that multiagent learning (MAL) should be more than multiagent reinforcement learning (MARL):
  - Cao et al. (2007); Stone (2007); Tuyls and Weiss (2012)
- Haven't the 1990s ideas materialized ?
- An still open question is: what exactly is meant with MAL?



## "Old days" Agenda for MAL

- Synergy between MASs and ML was of a broader nature, and the motivations for and questions around MAL were different
- Brazdil and colleagues in 1991: "Two rather different questions can be formulated in the context of studying ML in multi-agent systems. First, how can multi-agent systems benefit from machine learning. Second, how can machine learning benefit from considering multi-agent set-up. As multi-agent systems are by nature complex, machine learning techniques may be the only way to achieve a robust and versatile system."



## Compilations and reflections on MAL

- Brazdil and colleagues: see before
- Stone and Veloso (2000): survey on existing MAS techniques, emphasizing the use of ML
  - ML techniques: can be directly applied in multiagent scenarios, either by delimiting a part of the domain that only involves a single agent, or by focusing on learning issues that arise because of the multiagent aspect of a given domain
  - They listed learning approaches (before 2000) for some classes of problems along two dimensions: homogeneity and communication



## Stone and Veloso Survey

- homogeneous non-communicating agents:
  - NRL: stigmergy; local knowledge; game theory
  - RL: environment independent reinforcement acceleration (EIRA); Q-learning for foraging
- heterogeneous non-communicating agents:
  - NRL: genetic programming; genetic algorithms; case-base reasoning; game theory; competitive co-evolution
  - RL: multiagent RL for adaptive load balancing;
     Q-learning; Minimax-Q



## Stone and Veloso Survey

- homogeneous communicating agents:
  - NRL: distributed sensing
- heterogeneous communicating agents:
  - NRL: learning social behaviors; cooperative co-evolution; Bayesian learning
  - RL: multiagent Q-learning



### Distributed ML: Motivations Related to MASs

- As it seems, the "old days" agenda on putting together ML and MASs forming multiagent learning (MAL), which was much broader than just using RL, was kind of abandoned by the MASs community
- In the meantime, what has happened in the ML community
   ?
- Part of that agenda now runs under distributed ML
- This deals with a large amount of data, data that is distributed over many locations, and privacy issues
- Distribution and privacy issues are opportunities for the interaction between agents and ML!



### Distributed ML

- Foundations: ensemble learning
- Idea: build a set of classifiers, e.g., by training each one on different subsets of data and later combining them
- Ensemble learning suits well a distributed, MASs environment, especially regarding horizontal (regarding instances) partition



### Distributed ML

- Characteristics of ensembles:
  - use of different learning processes to train classifiers with different learning biases (diversity of methods);
  - 2 combination of different answers for the same problem (diversity in solutions);
  - ability to deal with large and distributed data sets (partitions of data can be allocated to different processors);
  - profit from distributed expertise (diversity in data)
- Algorithms for distributed ML are based on some kind of integration or combination mechanism that operates on the partial results found by distributed actors (e.g., classifiers)
- Arbiters and/or broadcasting of the local classifier are frequently employed
- Many of these issues are tackled by MASs



## Integration of MASs and distributed ML

- For integration MASs and distribute ML: two particular points are important
  - each ML algorithm has a bias: implies a preference for certain generalizations over others
  - different ML techniques use different representations of the attributes; it is hardly possible to have a common representation (at least not without losing information)
- What are the implications for MASs?



## Integration of MASs and distributed ML

- For classification tasks: agent-based solutions to reach the "ensemble effect"
- Agents can have different expertise or have access to different data, they may work together towards a consensus and more reliable prediction
- To address privacy and representation issues: agents do not exchange raw data (only the outputs) using an abstract representation (hypothesis over classes, etc.)
- Distributed ML is performed by first generating local models based on the distributed data analysis, and then adopting a strategy to combine them into a global model
- Collaborative learning: agents share information and perform negotiation to devise a coherent global model
- Second step combination of solutions is where MASs. Infection techniques have more room to be applied

### Integration of MASs and distributed ML

- Applications of agent-based ML are those dealing with:
  - heterogeneous and distributed data
  - data where ethical and privacy issues arise: medical data (diagnosis, treatment details, laboratory data, among others, which are provided by multiple and independent sources), fraud detection in financial organizations, etc.



### Agent-based ML

#### Issues

- heterogeneous and/or self-interested agents: Kargupta et al. (1999), Tozicka et al. (2007)
- exchange information during learning: Modi and Shen (2001); Santana et al. (2006); Bazzan (2013); Chaimontree et al. (2012); Wardeh et al. (2012)
- privacy: Stolfo et al. (1997); Silva et al. (2005); Modi and Shen (2001); Recamonde-Mendoza and Bazzan (2016)
- feature and parameters selection: Zhang and Wang (2012);
   Babu et al. (2009)
- negotiation: Chaimontree et al. (2012); Emele et al. (2012)



### Agent-based ML

### Techniques

- diversity of algorithms (classification): Kargupta et al. (1999); Recamonde-Mendoza and Bazzan (2016)
- diversity of algorithms (clustering): Chaimontree et al. (2010)
- hierarchical clustering: Kargupta et al. (1997)
- cluster ensemble: Agogino and Tumer (2006)

### Applications

- intrusion detection: Stolfo et al. (1997)
- bioinformatics: Bazzan (2009); Recamonde-Mendoza and Bazzan (2016)
- tracking / trajectories: Zhang and Wang (2012)



### ML in and for MASs

#### Issues

- heterogeneous agents: Nunes and Oliveira (2004); Brahmi et al. (2012); Bekkerman et al. (2007)
- negotiation: Hindriks and Tykhonov (2008)
- opponent modeling: Hindriks and Tykhonov (2008)

### Techniques

- multi-objective clustering: dos Santos et al. (2009)
- classification / regression: Emele et al. (2012); Şensoy et al. (2013)
- clustering: Pan et al. (2013); Brahmi et al. (2012); Ogston et al. (2003); Garruzzo and Rosaci (2008); Piraveenan et al. (2008)
- biologically inspired: Alam et al. (2009); Lemmens and Tuyls (2009); dos Santos and Bazzan (2012)



### ML in and for MASs

### Applications

- intrusion detection / web: Alam et al. (2009); Bekkerman et al. (2007); Brahmi et al. (2012)
- traffic / trajectories / maze: Fiosins et al. (2012); Lemmens and Tuyls (2009); Nunes and Oliveira (2004); Urban et al. (2010)
- sensor networks: Piraveenan et al. (2008)
- supply chain management / TAC: Kiekintveld et al. (2007)



L Agent-Based ML

### Main characteristics

- Majority of works: agents encapsulating ML algorithms in order to enhance data mining in applications such as credit card fraud detection system, intrusion detection, market segmentation, sensor networks, customer profiling, bioinformatics, etc.
- Many use classification or clustering algorithms
- Let us look at some of them...



Integration ML and MAS

Agent-Based ML

## **Agent-Based Classification**

- Modi and Shen (2001): decentralized algorithms based on collaborative learning for distributed classification tasks
  - agents learn their models individually based on a set of local features, collaborating with each other by exchange of information during the learning process in order to refine each others model
  - Agents' private data is never revealed: communication about individual training instance is performed in terms of their ids
  - At the end of the process, agents vote to decide the group's prediction
- Santana and colleagues (2006): agent-based neural network classifier; partially explore diversity among agents (agents have the same basic functioning, but different method's parameter values)
  - confidence-based negotiation: the agent with the highest .Interest confidence classifies unlabeled instances

Agent-Based ML

## **Agent-Based Classification**

- Recamonde-Mendoza and Bazzan (2016): extend Modi and Shen's work (recall: collaborative learning for distributed classification tasks) to explore variation of algorithms among agents (deal with heterogeneous agents); suitable for vertical partition
- Bazzan (2013): classification is combined with RL (states
  of the MDP are values of the attributes of the new instance
  to be classified; actions are the possible values of the
  target class)
- Wardeh et al. (2012): classification combined with argumentation: a group of agents argue about the classification of a given case according to their experience as recorded in individual local data sets

Integration ML and MAS
Agent-Based ML

- Standard clustering methods rely on central data structures
- Multiple agents can deal with multiple clustering criteria and/or multiple aspects of the data
- Privacy: only high-level information derived from data analysis is shared among agents



Agent-Based ML

- Kargupta et al. (1997): PADMA to deal with distributed data sources and hierarchical clustering
- Silva et al. (2005): agent-oriented algorithm for privacy-preserving clustering applied to sensor networks
- Tozicka et al. (2007): generic framework to deal with interaction heterogeneous and/or self-interested learners
- Chaimontree et al. (2010): agents use distinct clustering algorithm: K-means, K-nearest neighbors and DBSCAN
- Chaimontree et al. (2012): two phases involving 1. bidding for data points, 2. negotiation in which agents pass individual records to each other to improve the initial result
- Babu et al. (2009): Clustering combined with decision trees where agents do feature selection and use domain knowledge to generate a decision tree

- Agogino and Tumer (2006)
  - Ensemble of clusters without using the original data points that were used to generate these sets
  - Use of difference utilities (a.k.a. COIN or WLU; Tumer and Wolpert (2000)) to maximize the global utility of the clustering
  - Task of cluster ensemble is different from clustering
    - combines multiple clusterings, formed from different aspects of the same data set, into a single unified clustering
    - goal is to create a single clustering that best characterizes a set of clustering, without using the original data points
  - Preserves privacy



- Multi-objective clustering: one of the most interesting scenarios for using agents because it may involve competition, conflicts
  - dos Santos et al. (2009): MACC (multi ant colony clustering) inspired by ant colony optimization and multi-objective clustering
    - Simultaneously uses several ant colonies, each one aiming to optimize one particular objective
    - Find different shapes and sizes of clusters and different types of structures in a data set



LML in MASs

### Main Characteristics

- Majority of works aim at helping agents to predict behaviors of other agents or characteristics of the environment in which the agent acts
- Use of ML techniques is more diverse compared to the case of agent-based ML
- ML techniques frequently appear in combination with other Al techniques



### Various techniques used

- Nunes and Oliveira (2004):
  - heterogeneous learning agents improving their learning skills by communicating with members of other groups that are solving similar problems in different areas
  - Agents use various ML techniques (Q-learning, neural networks) as well as heuristics
  - Application: several sources during learning is used in a simplified traffic control problem
- Fiosins et al. (2012): application of bootstrap-based CUSUM in decentralized routing of vehicles
- Urban et al. (2010): expectation-maximization to build a Gaussian mixture model and train a HMM to detect anomalous trajectories



LML in MASs

## Various techniques used

- Şensoy et al. (2013): regression to discover patterns of interactions among agents in order to estimate trust
- Emele et al. (2012): decision trees extended with ontological reasoning, argumentation, and use of domain knowledge to support learning of policies
- Cetnarowicz et al. (1996): evolutionary approach for the task prediction to improve the performance of agents



## Clustering combined with other techniques

- Pan et al. (2013): clustering combined with KNN for labeling items in collaborative tagging and recommender systems
- Bekkerman et al. (2007): multiagent heuristic web searching algorithms for web page clustering agents
- Brahmi et al. (2012): association rules and clustering used for dealing with intrusion detection, where agents collect and analyze the network connections patterns
- Garruzzo and Rosaci (2008): clustering of agents based on similarity value that has lexical, structural and semantic components



LML in MASs

## Clustering combined with other techniques

- Ogston et al. (2003): clustering of agents with similar objectives or data
- Piraveenan et al. (2008): predictor for convergence time of cluster formation in sensor grids
- dos Santos and Bazzan (2012): swarm intelligence, bee dance metaphor to cluster agents in the domain of the RoboCup Rescue



└ML in MASs

### RL combined with GA

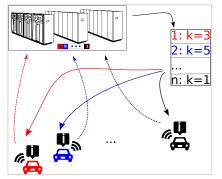
- Many real-world problems: conflict between desired performance of the system as a whole, and performance of individual components
- Example of congestion games: while a central authority is interested in optimizing the average travel time, drivers are interested in optimizing their own individual travel times
- Proposed solution: synergy between GA and RL
  - GA optimizes for the central authority (find an assignment of routes, one for each driver agent)
  - RL is used by driver agents to find a route that minimizes its travel time



LML in MASs

### RL combined with GA (cont.)

- Example of congestion games: while a central authority is interested in optimizing the average travel time, drivers are interested in optimizing their own individual travel times
- Proposed solution: synergy between GA and RL (Bazzan, 2018)





## Transition from single agent to multiagent

- Advantages...
- ... but also challenges:
  - Modal logics, mental states
  - Distributed problem solving
  - Decision making in complex, dynamic, and partially observable environments
  - Multiagent learning
  - Learning / adaptation
  - Self organization and/for task allocation
  - Mix of techniques
  - Synergy between various techniques



### Thank You!

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- Next slides contain references cited
- You find these slides at www.inf.ufrgs.br\~bazzan



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